

# Chapter 14

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# Frequency Response

By Eng. Emad Mahdy

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# Chapter 14 Laws:

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- 14.1 Introduction
- 14.2 Transfer Function
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- 14.6 Parallel Resonance
- 14.7 Passive Filters

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## 14.1 Introduction

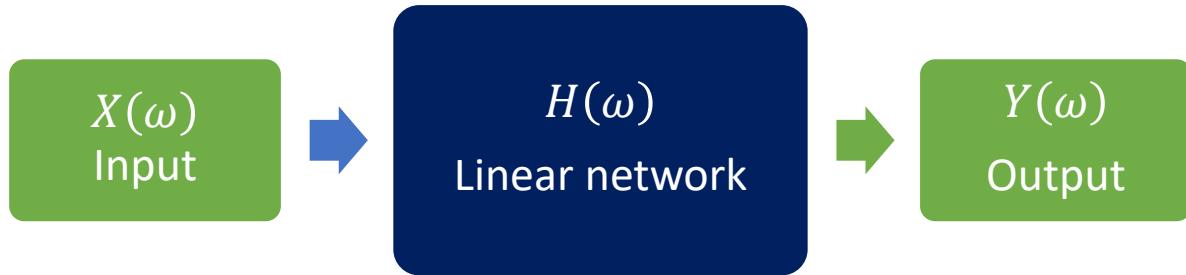
The **frequency response** of a circuit is the variation in its behavior with change in signal frequency.

استجابة التردد هو تغير سلوك الدائرة مع تغير الاشارة الداخلة لها

- frequency responses of circuits are used in many applications, especially **in communications and control systems**.  
تستخدم دوائر استجابة التردد في العديد من التطبيقات خاصة في الاتصالات وانظمة التحكم
- A specific application is in **electric filters** that block out or eliminate signals with unwanted frequencies and pass signals of the desired frequencies.  
أحد التطبيقات هو دائرة المرشح **electric filter** ويتم استخدامه للحصول على ترددات معينة من الدائرة  
وازالة ترددات اخرى
- Filters** are used in radio, TV, and telephone systems to separate one broadcast frequency from another.  
تستخدم دوائر المرشح في الراديو والتلفزيون

## 14.2 Transfer Function

Transfer function



where is:  $H(\omega) = \frac{Y(\omega)}{X(\omega)}$

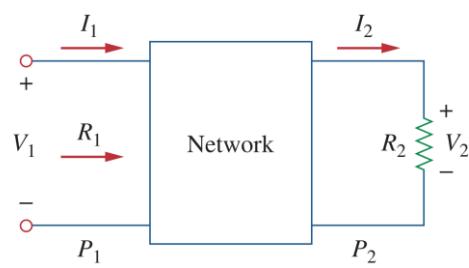
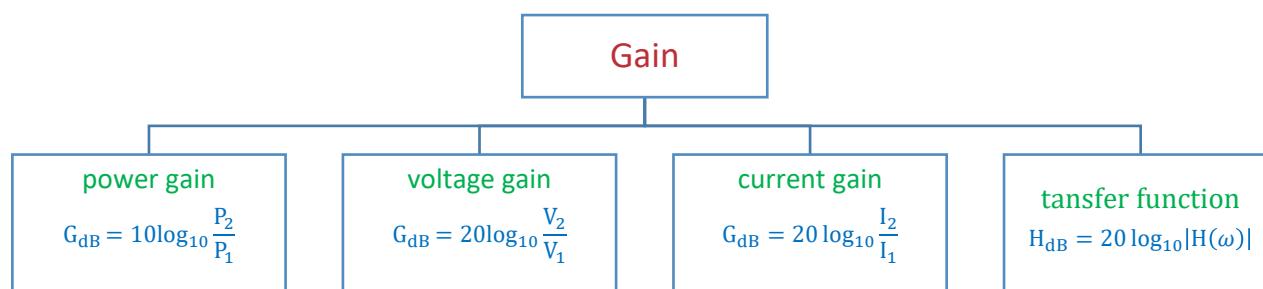
	Time-domain	Frequency domain
Input	$x(t)$	$X(\omega)$
Output	$y(t)$ [response]	$Y(\omega)$
Transfer function	$h(t)$ [impulse response]	$H(\omega)$ [transfer function]

poles and zeros:

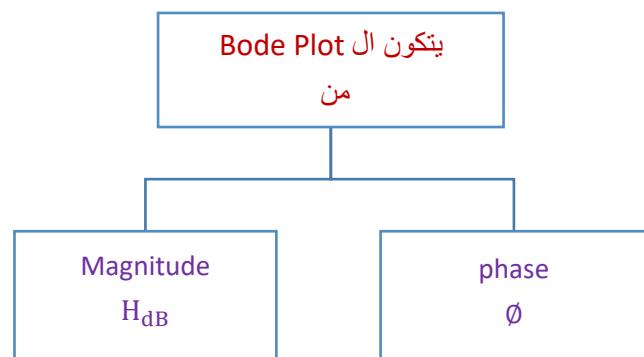
$$H(\omega) = \frac{N(\omega)}{D(\omega)}$$

- لو عاوز اجيبي ال zeros: نساوي البسط ب صفر ( $N(\omega) = 0$ ) ونحل المعادلة
- لو عاوز اجيبي ال poles: نساوي المقام ب صفر ( $D(\omega) = 0$ ) ونحل المعادلة

## 14.3 The Decibel Scale



## 14.4 Bode Plots



عندما يطلب في المسألة رسم ال bode plot فانه يطلب رسم شيئين:

Magnitude ▪

Phase ▪

أولاً نجعل ال الشكل القياسي  $H(s)$  transfer function على الشكل القياسي

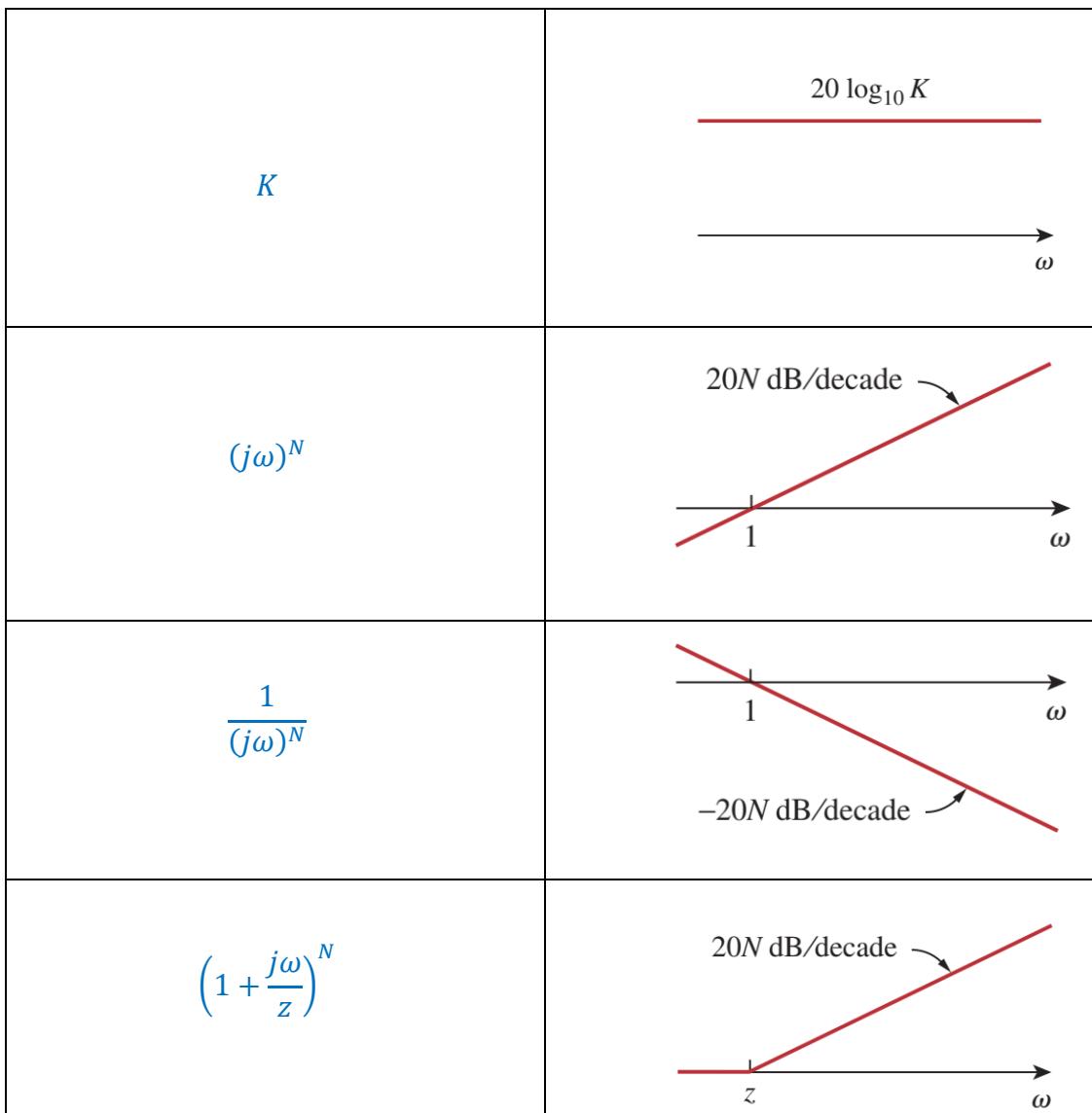
أي مقدار في البسط هو عبارة عن zero ▪

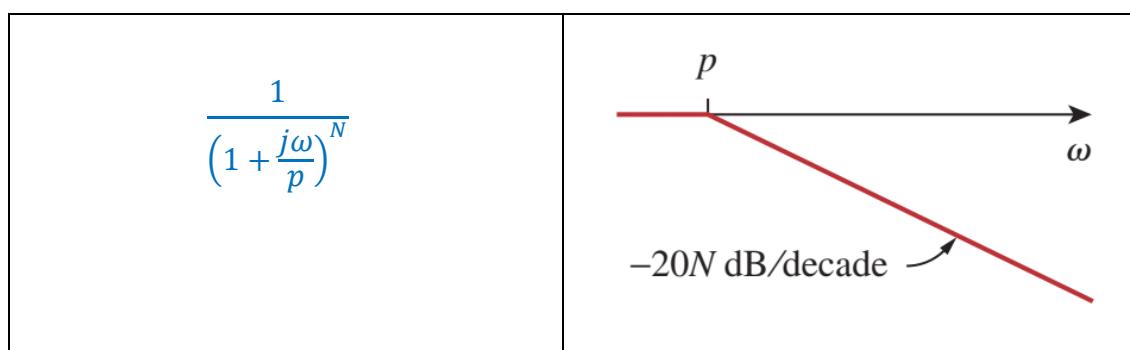
$$H(s) = \frac{K(j\omega) \left(1 + \frac{j\omega}{z}\right)}{\left(1 + \frac{j\omega}{p_1}\right) \left(1 + \frac{j\omega}{p_2}\right)}$$

أي مقدار في المقام هو عبارة عن pole ▪

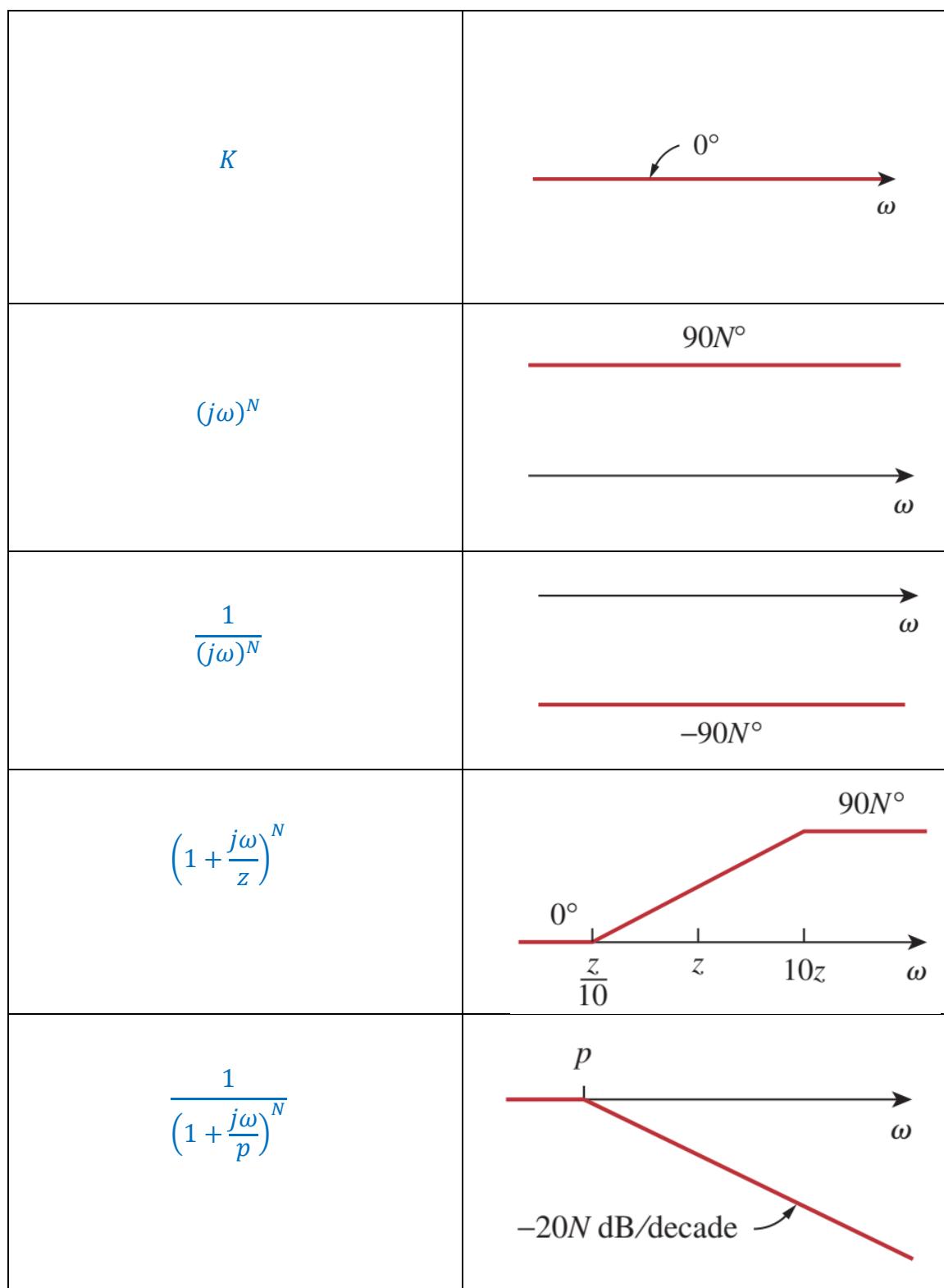
أي poles له ميل سالب ▪  
أي zero له ميل موجب ▪

نقوم برسم ال  $H_{dB}$  magnitude بالقواعد الآتية:





رسم ال  $\phi$  بالقواعد الآتية:

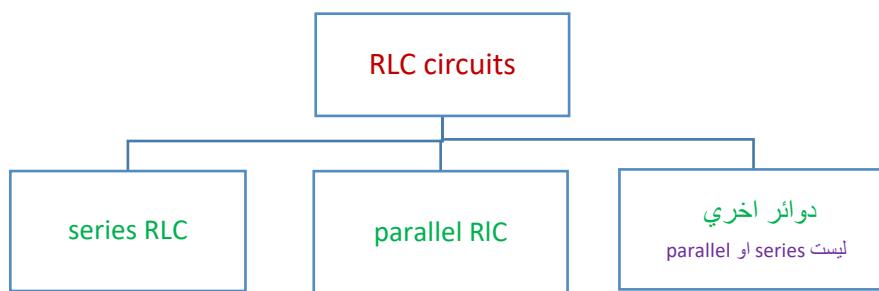


## 14.5 Series Resonance and 14.6 Parallel Resonance

دائرة الرنين resonance circuit

هي دائرة RLC تلاشى فيها المقاومة الناتجة عن ال  $L$  المقاومة الناتجة عن ال  $C$  وبالتالي تصبح المقاومة الوحيدة المؤثرة هي ال  $R$  وتصبح الدائرة عبارة عن purely resistive impedance

Series RLC circuits	Parallel RLC circuits
	$I = I_m \angle \theta$



ملخص قوانين series and parallel RLC circuits

## series and parallel RLC circuits ملخص قوانین

<b>Resonant frequency <math>\omega_0</math></b>	$\omega_0 = \frac{1}{\sqrt{LC}} \text{ rad/s}$
<b>Half-power frequencies <math>\omega_1, \omega_2</math></b>	$\omega_1 = -\frac{R}{2L} + \sqrt{\left(\frac{R}{2L}\right)^2 + \frac{1}{LC}}$ $\omega_2 = \frac{R}{2L} + \sqrt{\left(\frac{R}{2L}\right)^2 + \frac{1}{LC}}$ <p style="text-align: right;">حالة خاصة: عند <math>Q \geq 10</math></p> $\omega_1 \approx \omega_0 - \frac{B}{2}$ $\omega_2 \approx \omega_0 + \frac{B}{2}$
<b>Bandwidth, B</b>	<p style="text-align: center;"><b>RLC circuit</b></p> $B = \frac{\omega_0}{Q} = \omega_2 - \omega_1$ <pre> graph TD     A[RLC circuit] --&gt; B["B = ω₀ / Q = ω₂ - ω₁"]     B --&gt; C[series RLC circuits]     B --&gt; D[parallel RLC circuits]     C --- E["B = R / L"]     D --- F["B = 1 / RC"]   </pre>
<b>Quality factor, Q</b>	<p style="text-align: center;"><b>RLC circuit</b></p> $Q = \frac{\omega_0}{B}$ <pre> graph TD     A[RLC circuit] --&gt; B["Q = ω₀ / B"]     B --&gt; C[series RLC circuits]     B --&gt; D[parallel RLC circuits]     C --- E["Q = 1 / (ω₀ C R)"]     D --- F["Q = ω₀ C R"]   </pre>
<b>dissipated power at resonant frequency, P(<math>\omega_0</math>)</b>	$P(\omega_0) = \frac{1}{2} \frac{V_m^2}{R}$
<b>dissipated power at cut-off frequency, P(<math>\omega_1</math>), P(<math>\omega_2</math>)</b>	$P(\omega_1) = P(\omega_2) = \frac{1}{4} \frac{V_m^2}{R}$

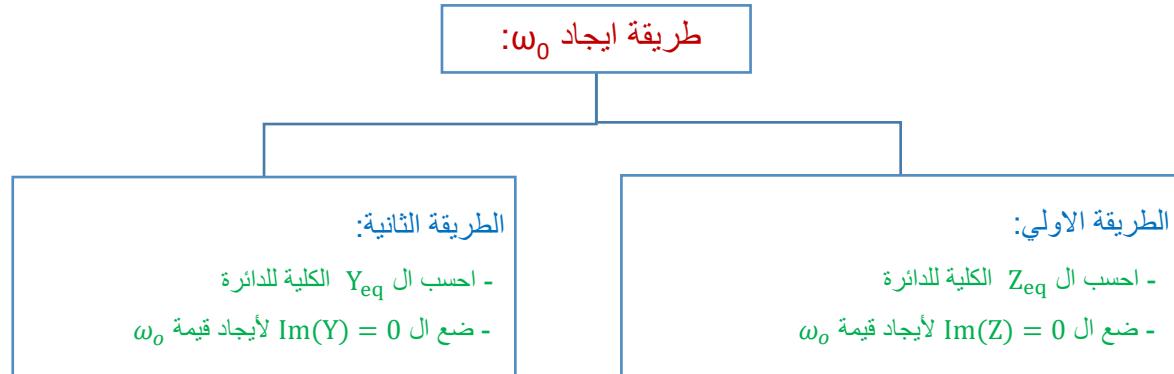
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بالنسبة لأي دائرة RLC أخرى (ليست series ولا parallel):



### ملاحظات على دوائر الرنين

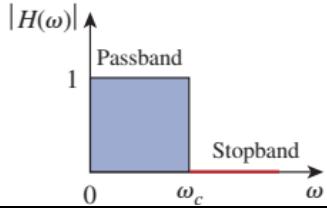
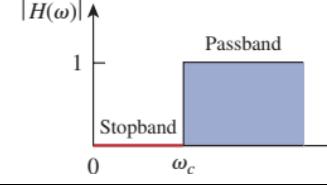
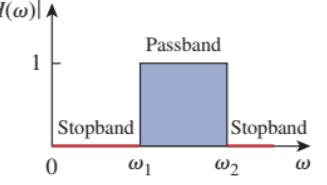
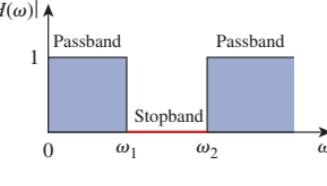
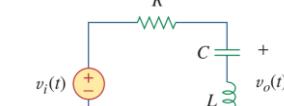
1. The impedance is purely resistive (the LC series combination acts like a short circuit)
2. The voltage and the current are in phase ( $p_f = 1$ ).

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## 14.7

أي passive filter يتكون من:

Passive filters = resistors + capacitors + Inductors.

passive Filters				
Filter نوع ال	شكل ال Filter	transfer function ال للفلتر	$\omega_c$	دائرة ال filter
low-pass filter		$H(\omega) = \frac{1}{1 + j\omega RC}$	$\omega_c = \frac{1}{RC}$	
high-pass filter		$H(\omega) = \frac{j\omega RC}{1 + j\omega RC}$	$\omega_c = \frac{1}{RC}$	
band-pass filter		$H(\omega) = \frac{R}{R + j(\omega L - \frac{1}{\omega C})}$	$\omega_o = \frac{1}{\sqrt{LC}}$	
band-stop filter		$H(\omega) = \frac{j(\omega L - \frac{1}{\omega C})}{R + j(\omega L - \frac{1}{\omega C})}$	$\omega_o = \frac{1}{\sqrt{LC}}$	

Type of filter	$H(0)$	$H(\infty)$	$H(\omega_0)$ or $H(\omega_c)$
Low-pass	1	0	$\frac{1}{\sqrt{2}}$
High-pass	0	1	$\frac{1}{\sqrt{2}}$
Band-pass	0	0	1
Band-stop	1	1	0

ملاحظة هامة:

ال resonance RLC circuit م عبارة عن series RLC circuit وband-stop filters و Band-pass filter يمكن التعامل معهم بنفس القوانين دوائر

## 14.8 Active Filters

اي active filter يتكون من:

Passive filters = resistors + capacitors + OpAmps.

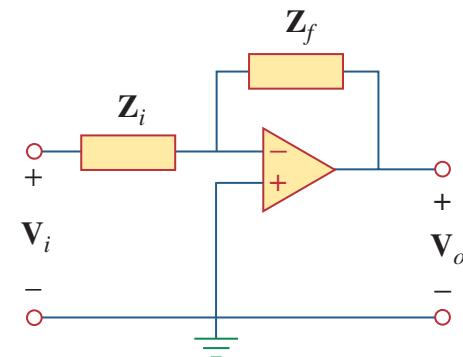
There are three major limitations to the passive filters

1. they cannot generate gain greater than 1; passive elements cannot add energy to the network.
2. they may require bulky and expensive inductors.
3. they perform poorly at frequencies below the audio frequency range but, passive filters are useful at high frequencies.
4. Active circuits are often smaller and less expensive (because they do not require inductors).
5. active filters can be combined with buffer amplifiers to isolate each stage of the filter from source and load impedance effects.

Filters	Passive Filters	Active Filters
Gain	cannot generate Gain greater than 1. (passive elements cannot add energy to the network.)	Can generate gain greater than one (using buffer amplifiers)
Inductors	Require Inductors	they do not require inductors (so, they are smaller and less expensive)
High frequencies	passive filters can operate at high frequencies	The practical limit of most active filters can operate below Frequency $\leq 100$ kHz
Components	Passive filters = resistors + capacitors + Inductors.	Active filters = resistors + capacitors + opamps.

## First Order Filters

الشكل العام لدائرة أي فلتر من الدرجة الأولى first order filter



First order Filter	نوع ال filter transfer function ال	Corner frequency $\omega_c$	Gain	دائرة ال filter
low-pass filter	$H(\omega) = -\frac{R_f}{R_i} \frac{1}{1 + j\omega C_f R_f}$	$\omega_c = \frac{1}{C_f R_f}$	dc gain (at $\omega \rightarrow 0$ ) $K = -\frac{R_f}{R_i}$	
high-pass filter	$H(\omega) = -\frac{j\omega C_i R_f}{1 + j\omega C_i R_i}$	$\omega_c = \frac{1}{C_i R_i}$	dc gain (at $\omega \rightarrow \infty$ ) $K = -\frac{R_f}{R_i}$	
band-pass filter	$H(\omega) = -\frac{R_f}{R_i} \frac{j\omega\omega_2}{(\omega_1 + j\omega)(\omega_2 + j\omega)}$	$\omega_0 = \sqrt{\omega_1\omega_2}$	passband gain $K = \frac{R_f}{R_i} \frac{\omega_2}{\omega_1 + \omega_2}$	 Detailed description: The circuit diagram shows a three-stage filter. Stage 1 is a low-pass filter with a corner frequency of omega_1, consisting of a resistor R1 and a capacitor C1 in series with the input vi. Stage 2 is a high-pass filter with a corner frequency of omega_2, consisting of a resistor R2 and a capacitor C2 in parallel with the output of Stage 1. Stage 3 is an inverter with a resistor Rf, providing the final output vo.
band-stop filter	غير مهم	غير مهم	غير مهم	غير مهم

## 14.9 Scaling

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